



St Mary's Primary School

UKS2 Calculation Policy

Autumn 2023

The following pages show the progression in calculation (addition, subtraction, multiplication and division) and how this works in line with the National Curriculum. The consistent use of the CPA (concrete, pictorial, abstract) approach helps children develop mastery across all the operations in an efficient and reliable way. This policy shows how these methods develop children's confidence in their understanding of both written and mental methods.

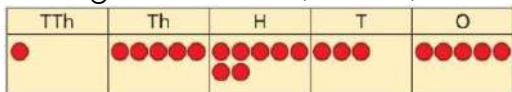
<p>Addition and subtraction: Children build on their column methods to add and subtract numbers with up to seven digits, and they adapt the methods to calculate efficiently and effectively with decimals, ensuring understanding of place value at every stage. Children compare and contrast methods, and they select mental methods or jottings where appropriate and where these are more likely to be efficient or accurate when compared with formal column methods. Bar models are used to represent the calculations required to solve problems and may indicate where efficient methods can be chosen.</p>	<p>Multiplication and division: Building on their understanding, children develop methods to multiply up to 4-digit numbers by single-digit and 2-digit numbers. Children develop column methods with an understanding of place value, and they continue to use the key skill of unitising to multiply and divide by 10, 100 and 1,000. Written division methods are introduced and adapted for division by single-digit and 2-digit numbers and are understood alongside the area model and place value. In Year 6, children develop a secure understanding of how division is related to fractions. Multiplication and division of decimals are also introduced and refined in Year 6.</p>
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Year 5			
Addition			
	Concrete	Pictorial	Abstract

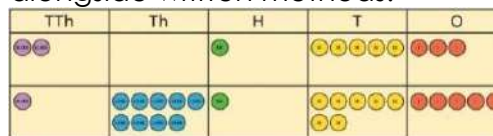
Column addition with whole numbers

Use place value equipment to represent additions. Place value counters/ plain counters are the most effective concrete resources.

Add a row of counters onto the place value grid to show $15,735 + 4,012$.



Represent additions, using place value equipment on a place value grid alongside written methods.



I need to exchange 10 tens for a 100.

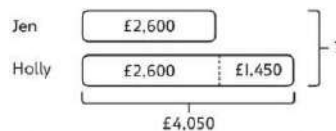
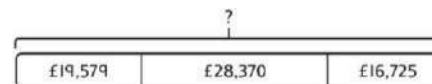
$$\begin{array}{r}
 \text{TTh Th H T O} \\
 2 \ 0 \ 1 \ 5 \ 3 \\
 + 1 \ 9 \ 1 \ 7 \ 5 \\
 \hline
 3 \ 9 \ 3 \ 2 \ 8
 \end{array}$$

Use column addition, including exchanges.

$$\begin{array}{r}
 \text{TTh Th H T O} \\
 1 \ 9 \ 1 \ 7 \ 5 \\
 + 1 \ 8 \ 4 \ 1 \ 7 \\
 \hline
 3 \ 7 \ 5 \ 9 \ 2
 \end{array}$$

Representing additions

Bar models represent addition of two or more numbers in the context of problem solving.


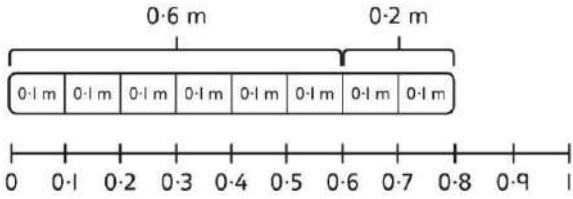
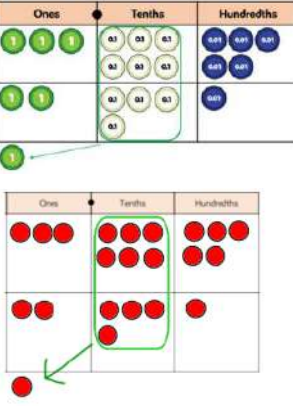
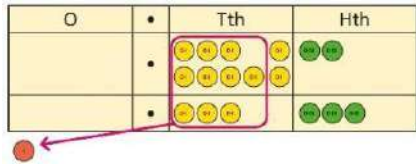
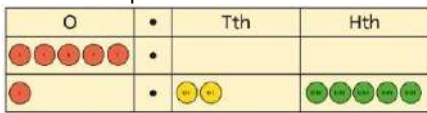


$$\begin{array}{r}
 \text{Th H T O} \\
 2 \ 6 \ 0 \ 0 \\
 + 1 \ 4 \ 5 \ 0 \\
 \hline
 4 \ 0 \ 5 \ 0
 \end{array}
 \qquad
 \begin{array}{r}
 \text{Th H T O} \\
 2 \ 6 \ 0 \ 0 \\
 + 4 \ 0 \ 5 \ 0 \\
 \hline
 6 \ 6 \ 5 \ 0
 \end{array}$$

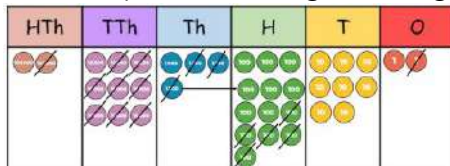
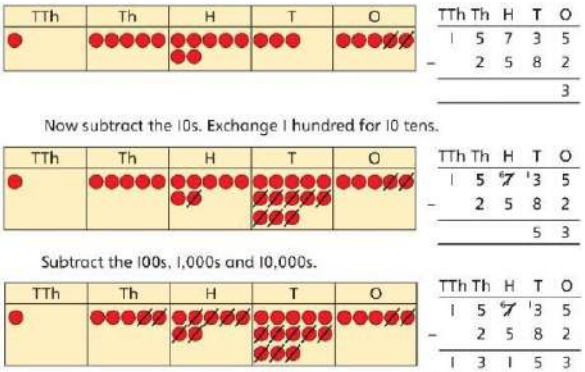
Use approximation to check whether answers are reasonable.

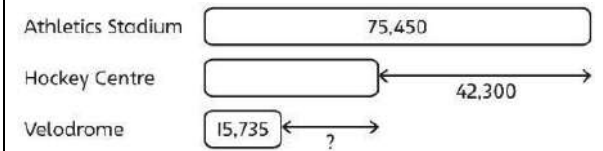
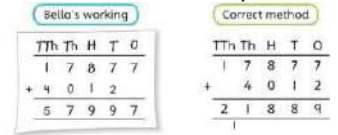
$$\begin{array}{r}
 \text{TTh Th H T O} \\
 2 \ 3 \ 4 \ 0 \ 5 \\
 + \ 7 \ 8 \ 9 \ 2 \\
 \hline
 2 \ 0 \ 2 \ 9 \ 7
 \end{array}
 \qquad
 \begin{array}{r}
 \text{TTh Th H T O} \\
 2 \ 3 \ 4 \ 0 \ 5 \\
 + \ 7 \ 8 \ 9 \ 2 \\
 \hline
 3 \ 1 \ 2 \ 9 \ 7
 \end{array}$$

I will use $23,000 + 8,000$ to check.

<p>Adding tenths</p>	<p>Link measure with addition of decimals.</p> <p>Two lengths of fencing are 0.6 m and 0.2 m. How long are they when added together?</p> <p>0.6 m 0.2 m</p> 	<p>Use a bar model with a number line to add tenths.</p>  <p>$0.6 + 0.2 = 0.8$ 6 tenths + 2 tenths = 8 tenths</p>	<p>Understand the link with adding fractions.</p> $\frac{6}{10} + \frac{2}{10} = \frac{8}{10}$ <p>6 tenths + 2 tenths = 8 tenths $0.6 + 0.2 = 0.8$</p>
<p>Adding decimals using column addition</p>	<p>Use place value equipment to represent additions.</p> <p>Show $0.23 + 0.45$ using place value counters.</p> <p>Place value counters and plain counters on a place value grid are the most effective manipulatives when adding decimals with 1, 2 and then 3 decimal places.</p> <p>$3.65 + 2.41$</p> 	<p>Use place value equipment on a place value grid to represent additions.</p> <p>Represent exchange where necessary.</p>  <p>Include examples where the numbers of decimal places are different.</p> 	<p>Add using a column method, ensuring that children understand the link with place value.</p> $\begin{array}{r} 0.92 \\ + 0.45 \\ \hline 1.37 \end{array}$ <p>Include exchange where required, alongside an understanding of place value.</p> $\begin{array}{r} 0.92 \\ + 0.33 \\ \hline 1.25 \end{array}$ <p>Include additions where the numbers of decimal places are different.</p> <p>$3.4 + 0.65 = ?$</p> $\begin{array}{r} 3.40 \\ + 0.65 \\ \hline \end{array}$

Subtraction

	Concrete	Pictorial	Abstract
<p>Column subtraction with whole numbers</p>	<p>Place value counters or plain counters on a place value grid are the most effective concrete resource when subtracting numbers with more than 4 digits.</p> <p>Build on place value grids using counters.</p> 	<p>Represent the stages of the calculation using place value equipment on a grid alongside the calculation, including exchanges where required.</p> <p>$15,735 - 2,582 = 13,153$</p> 	<p>Use column subtraction methods with exchange where required.</p> $ \begin{array}{r} \text{TTh Th H T O} \\ \underline{15\,735} \\ - \underline{2\,582} \\ \hline 13\,153 \end{array} $ <p>$62,097 - 18,534 = 43,563$</p>

<p>Checking strategies and representing subtractions</p>		<p>Bar models represent subtractions in problem contexts, including 'find the difference'.</p> 	<p>Children can explain the mistake made when the columns have not been ordered correctly.</p>  <p>Use approximation to check calculations.</p> <p><i>I calculated 18,000 + 4,000 mentally to check my subtraction.</i></p>
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<p>Choosing efficient methods</p>			<p>To subtract two large numbers that are close, children find the difference by counting on. $2,002 - 1,995 = ?$</p>  <p>Use addition to check subtractions.</p> <p><i>I calculated $7,546 - 2,355 = 5,191$.</i></p> <p><i>I will check using the inverse.</i></p>
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Subtracting decimals

Explore complements to a whole number by working in the context of length.



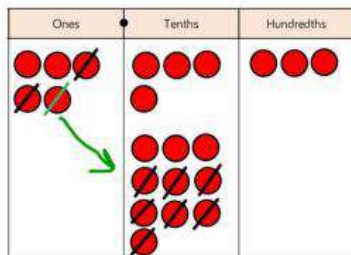
$$1 \text{ m} - \square \text{ m} = \square \text{ m}$$

$$1 - 0.49 = ?$$

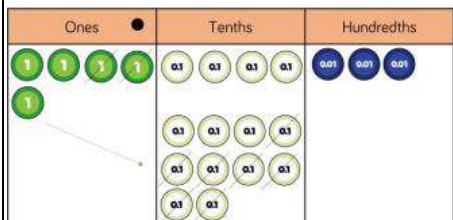
Place value counters and plain counters on a place value grid are the most effective manipulative when subtracting decimals with 1, 2 and then 3 decimal places.

Ensure children have experience of subtracting decimals with a variety of decimal places. This includes putting this into context

when subtracting money and other measures.



$$5.43 - 2.7$$



Use a place value grid to represent the stages of column subtraction, including exchanges where required.

$$5.74 - 2.25 = ?$$



$$\begin{array}{r} \text{O} \cdot \text{Tth} \text{ Hth} \\ 5 \cdot 7 \ 4 \\ - 2 \cdot 2 \ 5 \\ \hline \end{array}$$

Exchange 1 tenth for 10 hundredths.



$$\begin{array}{r} \text{O} \cdot \text{Tth} \text{ Hth} \\ 5 \cdot 6 \ 14 \\ - 2 \cdot 2 \ 5 \\ \hline \end{array}$$

Now subtract the 5 hundredths.



$$\begin{array}{r} \text{O} \cdot \text{Tth} \text{ Hth} \\ 5 \cdot 6 \ 14 \\ - 2 \cdot 2 \ 5 \\ \hline \cdot \ 9 \end{array}$$

Now subtract the 2 tenths, then the 2 ones.

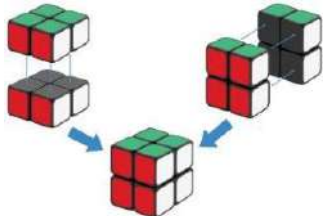

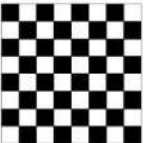
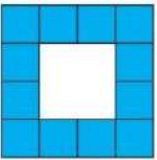


$$\begin{array}{r} \text{O} \cdot \text{Tth} \text{ Hth} \\ 5 \cdot 6 \ 14 \\ - 2 \cdot 2 \ 5 \\ \hline 3 \cdot 4 \ 9 \end{array}$$

Use column subtraction, with an understanding of place value, including subtracting numbers with different numbers of decimal places.




$$3.921 - 3.75 = ?$$

$$\begin{array}{r} \text{O} \cdot \text{Tth} \text{ Hth} \text{ Thth} \\ 3 \cdot 9 \ 2 \ 1 \\ - 3 \cdot 7 \ 5 \ 0 \\ \hline \cdot \end{array}$$

	Concrete	Pictorial	Abstract
Understanding factors	<p>Use cubes or counters to explore the meaning of 'square numbers'.</p> <p><i>25 is a square number because it is made from 5 rows of 5.</i></p> <p>Use cubes to explore cube numbers.</p>  <p><i>8 is a cube number.</i></p> <p>Use arrays of counters to understand factors.</p>  <p><i>The factors of 12 are 1 and 12, 2 and 6, 3 and 4.</i></p>	<p>Use images to explore examples and nonexamples of square numbers.</p>  <p>$8 \times 8 = 64$ $8^2 = 64$</p>  <p><i>12 is not a square number, because you cannot multiply a whole number by itself to make 12.</i></p>	<p>Understand the pattern of square numbers in the multiplication tables.</p> <p>Use a multiplication grid to circle each square number. Can children spot a pattern?</p> <p>Record in factor pairs.</p> <p>The factors of 12 are 1 and 12 2 and 6 3 and 4</p>

Multiplying by 10, 100 and 1,000

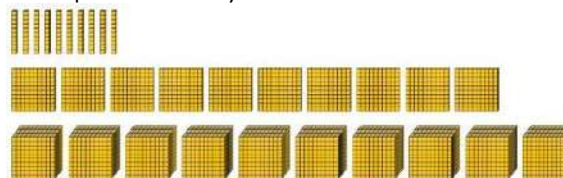
Use place value equipment to multiply by 10, 100 and 1,000 by unitising.

$4 \times 1 = 4 \text{ ones} = 4$	
$4 \times 10 = 4 \text{ tens} = 40$	
$4 \times 100 = 4 \text{ hundreds} = 400$	

HTh	TTh	Th	H	T	O
			● ●	● ● ●	● ● ● ●

Concrete manipulatives such as place value charts and counters and Gattegno charts should be used to support understanding, using children's knowledge of the relationship between digits in given rows/columns.

Understand the effect of repeated multiplication by 10.



100,000	200,000	300,000	400,000	500,000	600,000	700,000	800,000	900,000
10,000	20,000	30,000	40,000	50,000	60,000	70,000	80,000	90,000
1,000	2,000	3,000	4,000	5,000	6,000	7,000	8,000	9,000
100	200	300	400	500	600	700	800	900
10	20	30	40	50	60	70	80	90
1	2	3	4	5	6	7	8	9

Understand how exchange relates to the digits when multiplying by 10, 100 and 1,000.

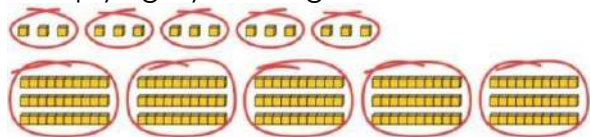
H	T	O
	1	7

$17 \times 10 = 170$
 $17 \times 100 = 17 \times 10 \times 10 = 1,700$
 $17 \times 1,000 = 17 \times 10 \times 10 \times 10 = 17,000$

Children need to be aware that the effect of multiplying by 10 twice is the same as multiplying by 100 and that multiplying by 10 three times is the same as multiplying by 1,000. Children should be comfortable with the language of "10 times the size of", "100 times the size of" and "1,000 times the size of".

Multiplying by multiples of 10, 100 and 1,000

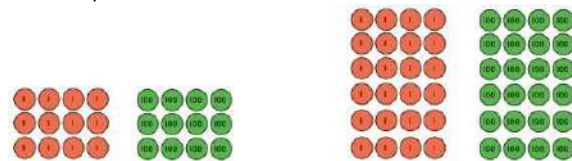
Use place value equipment to explore multiplying by unitising.



5 groups of 3 ones is 15 ones.
5 groups of 3 tens is 15 tens.

So, I know that 5 groups of 3 thousands would be 15 thousands.

Use place value equipment to represent how to multiply by multiples of 10, 100 and 1,000.



$$4 \times 3 = 12$$

$$4 \times 300 = 1,200$$

$$6 \times 4 = 24$$

$$6 \times 400 = 2,400$$

Use known facts and unitising to multiply.

$$5 \times 4 = 20$$

$$5 \times 40 = 200$$

$$5 \times 400 = 2,000$$

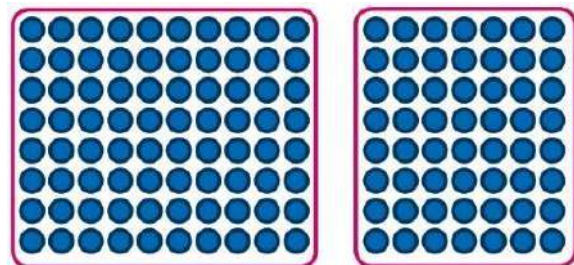
$$5 \times 4,000 = 20,000$$

$$5,000 \times 4 = 20,000$$

Multiplying up to 4-digit numbers by a single digit

Explore how to use partitioning to multiply efficiently.

$$8 \times 17 = ?$$



$$8 \times 10 = 80$$

$$8 \times 7 = 56$$

$$80 + 56 = 136$$

$$\text{So, } 8 \times 17 = 136$$

When multiplying 4-digit numbers, place value counters are the best manipulative to use to support children in their understanding of the formal written method.

Represent multiplications using place value equipment and add the 1s, then 10s, then 100s, then 1,000s.

$$163 \times 5$$

	H	T	O
100		10 10 10 10 10	1 1 1 1
100		10 10 10 10 10	1 1 1 1
100		10 10 10 10 10	1 1 1 1
100		10 10 10 10 10	1 1 1 1
100		10 10 10 10 10	1 1 1 1

$$1826 \times 3$$

Thousands	Hundreds	Tens	Ones
1000	100 100 100 100	10 10	1 1 1 1
1000	100 100 100 100	10 10	1 1 1 1
1000	100 100 100 100	10 10	1 1 1 1
1000	100 100 100 100	10 10	1 1 1 1

Use an area model and then add the parts.

	100	60	3
5	$100 \times 5 = 500$	$60 \times 5 = 300$	$3 \times 5 = 15$

Use a column multiplication, including any required exchanges.

$$\begin{array}{r} 136 \\ \times \quad 6 \\ \hline 816 \\ \underline{\quad 23} \end{array}$$

Multiplying 2digit numbers by 2-digit numbers

Partition one number into 10s and 1s, then add the parts.

$23 \times 15 = ?$



$10 \times 15 = 150$



$10 \times 15 = 150$



$3 \times 15 = 45$

There are 345 bottles of milk in total.

$23 \times 15 = 345$

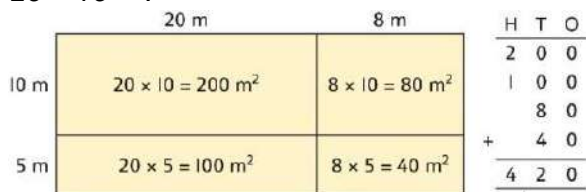
	H	T	O
	1	5	0
	1	5	0
+		4	5
	3	4	5

When multiplying a multi-digit number by 2-digits, use the area model to help children understand the size of the numbers they are using. This links to finding the area of a rectangle by finding the space covered by the Base 10.

22×31

Use an area model and add the parts.

$28 \times 15 = ?$



$28 \times 15 = 420$

×	20	2
30	600	60
1	20	2

grid method

The grid method matches the area model as an initial written method before moving on to the formal written multiplication method.

Use column multiplication, ensuring understanding of place value at each stage.

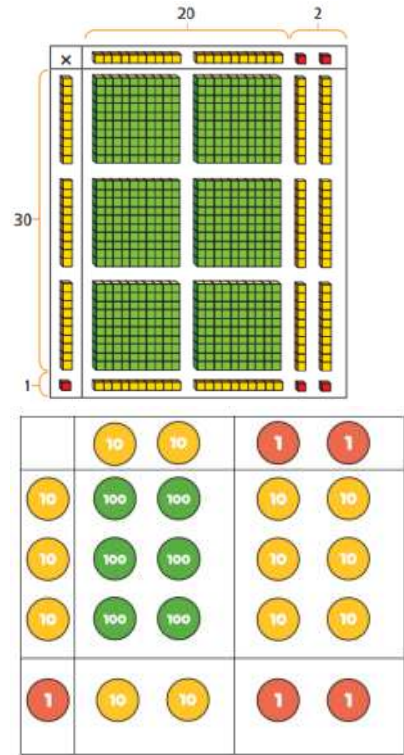
$34 \times 7 = 238$

$34 \times 20 = 680$

$34 \times 7 = 238$

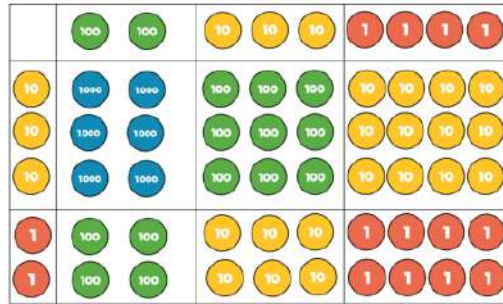
$34 \times 20 = 680$

$34 \times 27 = 918$



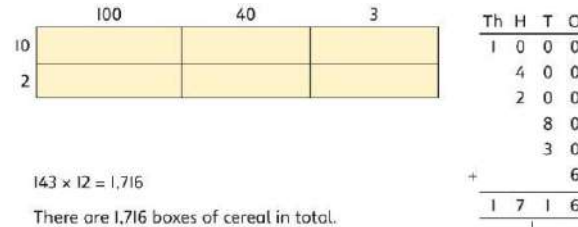
Multiplying up to 4-digits by 2-digits

Children can continue to use the area model when multiplying 3-digits by 2-digits. Place value counters become more efficient to use.



234×32

Use the area model then add the parts.



$143 \times 12 = 1,716$

234×32

\times	200	30	4
30	6,000	900	120
2	400	60	8

Children should now move towards the formal written method, seeing the links with the grid method.

Use column multiplication, ensuring understanding of place value at each stage.

$$\begin{array}{r} 143 \\ \times 12 \\ \hline 286 \\ 1430 \\ \hline 1716 \end{array}$$

143×2
 143×10
 143×12

Progress to include examples that require multiple exchanges as understanding, confidence and fluency build.

$1,274 \times 32 = ?$

First multiply 1,274 by 2.

$$\begin{array}{r} 1274 \\ \times 32 \\ \hline 2548 \end{array}$$

$1,274 \times 2$

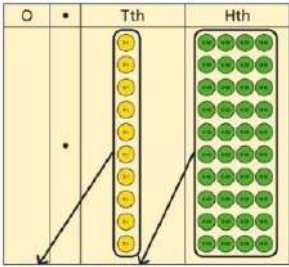

Then multiply 1,274 by 30.

$$\begin{array}{r} 1274 \\ \times 32 \\ \hline 2548 \\ 38220 \end{array}$$

$1,274 \times 2$
 $1,274 \times 30$



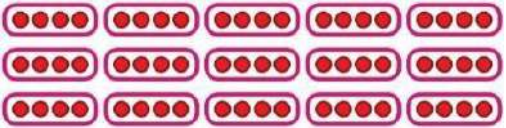
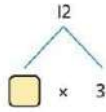
Finally, find the total.

			$ \begin{array}{r} 1\ 2\ 7\ 4 \\ \times \quad \quad 3\ 2 \\ \hline 2\ 5\ 4\ 8 \quad 1,274 \times 2 \\ 3\ 8\ 2\ 2\ 0 \quad 1,274 \times 30 \\ \hline 4\ 0\ 7\ 6\ 8 \\ \hline 1,274 \times 32 = 40,768 \end{array} $
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<p>Multiplying decimals by 10, 100 and 1,000</p>	<p>Use place value equipment to explore and understand the exchange of 10 tenths, 10 hundredths or 10 thousandths.</p>	<p>Represent multiplication by 10 as exchange on a place value grid.</p>  <p>$0.14 \times 10 = 1.4$</p>	<p>Understand how this exchange is represented on a place value chart.</p>  <p> $2.5 \times 10 = 25$ $2.5 \times 100 = 250$ $2.5 \times 1,000 = 2,500$ </p>
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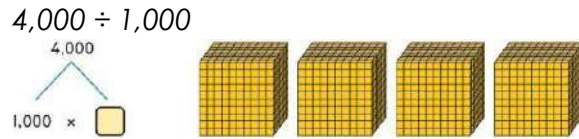
Division

	Concrete	Pictorial	Abstract
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<p>Understanding factors and prime numbers</p>	<p>Use counters to explore the factors of a given number.</p>  <p>$24 \div 3 = 8$ $24 \div 8 = 3$ 8 and 3 are factors of 24 because they divide 24 exactly. $24 \div 5 = 4$ remainder 4.</p>  <p>5 is not a factor of 24 because there is a remainder.</p>	<p>Understand that prime numbers are numbers with exactly two factors.</p> <p>$13 \div 1 = 13$ $13 \div 2 = 6 \text{ r } 1$ $13 \div 4 = 4 \text{ r } 1$</p> <p>1 and 13 are the only factors of 13. 13 is a prime number.</p>	<p>Understand how to recognise prime and composite numbers.</p> <p><i>I know that 31 is a prime number because it can be divided by only 1 and itself without leaving a remainder.</i></p> <p><i>I know that 33 is not a prime number as it can be divided by 1, 3, 11 and 33.</i></p> <p><i>I know that 1 is not a prime number, as it has only 1 factor.</i></p>
<p>Understanding inverse operations and the link with multiplication, grouping and sharing</p>	<p>Use equipment to group and share and to explore the calculations that are present.</p> <p><i>I have 28 counters.</i></p> <p><i>I made 7 groups of 4. There are 28 in total.</i></p> <p><i>I have 28 in total. I shared them equally into 7 groups. There are 4 in each group.</i></p> <p><i>I have 28 in total. I made groups of 4. There are 7 equal groups.</i></p>	<p>Represent multiplicative relationships and explore the families of division facts.</p>  <p>$60 \div 4 = 15$ $60 \div 15 = 4$</p>	<p>Represent the different multiplicative relationships to solve problems requiring inverse operations.</p> <p>$12 \div 3 = \square$ $12 \div \square = 3$ $\square \times 3 = 12$ $\square \div 3 = 12$</p>  <p>Understand missing number problems for division calculations and know how to solve them using inverse operations.</p> <p>$22 \div ? = 2$ $22 \div 2 = ?$ $? \div 2 = 22$ $? \div 22 = 2$</p>

Dividing whole numbers by 10, 100 and 1,000

Use place value equipment to support unitising for division.



4,000 is 4 thousands.

$$4 \times 1,000 = 4,000$$

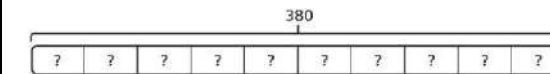
So, $4,000 \div 1,000 = 4$

HTh	TTh	Th	H	T	O
	●	●●	●●●		

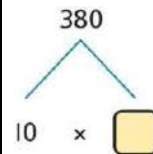
- 12300 ÷ 10
- 12300 ÷ 100
- 12300 ÷ 1000

Place value charts, counters and Gattegno charts can be used to support understanding, using children's knowledge of relationships between rows and columns. Children should be comfortable with the language of "one-tenth the size of", "one-hundredth the size of" and "one-thousandth the size of".

Use a bar model to support dividing by unitising.



$$380 \div 10 = 38$$



380 is 38 tens.
 $38 \times 10 = 380$
 $10 \times 38 = 380$
 So, $380 \div 10 = 38$

Understand how and why the digits change on a place value grid when dividing by 10, 100 or 1,000.

Th	H	T	O
3	2	0	0

$$3,200 \div 100 = ?$$

3,200 is 3 thousands and 2 hundreds.

$$200 \div 100 = 2$$

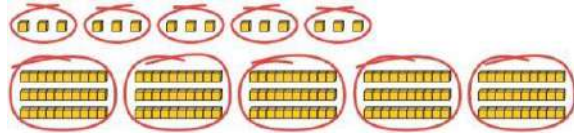
$$3,000 \div 100 = 30$$

$$3,200 \div 100 = 32$$

So, the digits will move two places to the right.

Dividing by multiples of 10, 100 and 1,000

Use place value equipment to represent known facts and unitising.



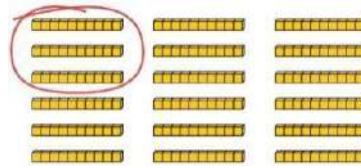
15 ones put into groups of 3 ones. There are 5 groups.

$$15 \div 3 = 5$$

15 tens put into groups of 3 tens. There are 5 groups.

$$150 \div 30 = 5$$

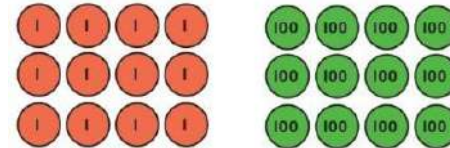
Represent related facts with place value equipment when dividing by unitising.



180 is 18 tens.

18 tens divided into groups of 3 tens. There are 6 groups.

$$180 \div 30 = 6$$



12 ones divided into groups of 4. There are 3 groups.

12 hundreds divided into groups of 4 hundreds. There are 3 groups.

$$1200 \div 400 = 3$$

Reason from known facts, based on understanding of unitising. Use knowledge of the inverse relationship to check.

$$3,000 \div 5 = 600$$

$$3,000 \div 50 = 60$$

$$3,000 \div 500 = 6$$

$$5 \times 600 = 3,000$$

$$50 \times 60 = 3,000$$

$$500 \times 6 = 3,000$$

Dividing up to four digits by a single digit using short division

When using the short division method, children use grouping. Starting with the largest place value, they group by the divisor.

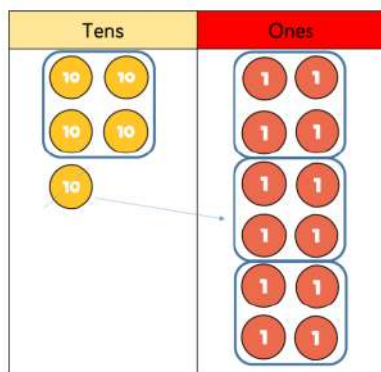
Explore grouping using place value equipment.

$$268 \div 2 = ?$$

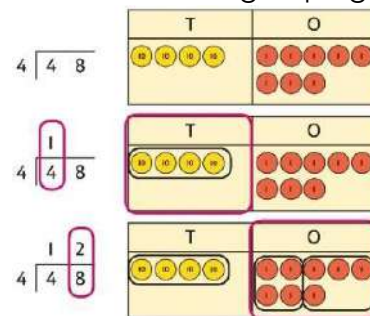
*There is 1 group of 2 hundreds.
There are 3 groups of 2 tens.
There are 4 groups of 2 ones.*

$$264 \div 2 = 134$$

$$52 \div 4 =$$



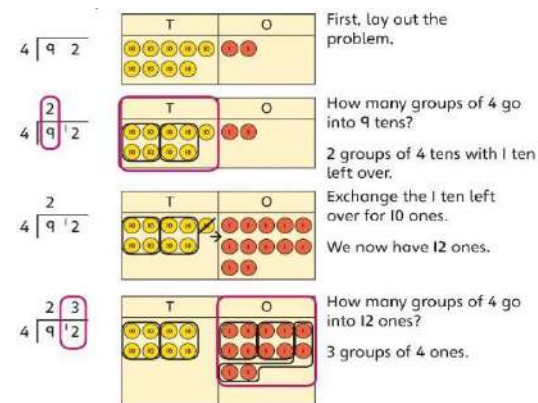
Use place value equipment on a place value grid alongside short division. The model uses grouping.



Lay out the problem as a short division.

*There is 1 group of 4 in 4 tens.
There are 2 groups of 4 in 8 ones.*

Work with divisions that require exchange.



Use short division for up to 4-digit numbers divided by a single digit.

$$\begin{array}{r} 0556 \\ 7 \overline{) 38942} \end{array}$$

$$3,892 \div 7 = 556$$

Use multiplication to check.

$$556 \times 7 = ?$$

$$6 \times 7 = 42$$

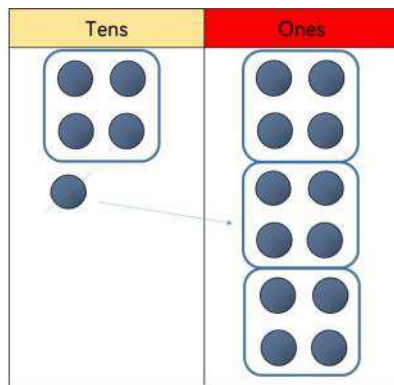
$$50 \times 7 = 350$$

$$500 \times 7 = 3500$$

$$3,500 + 350 + 42 = 3,892$$

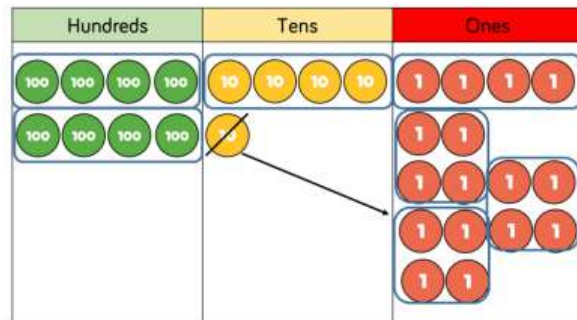
Children should be encouraged to move away from the concrete and pictorial when dividing numbers with multiple exchanges

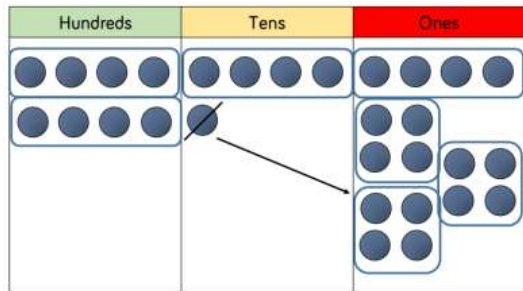
	4	2	6	6
2	8	5	13	12



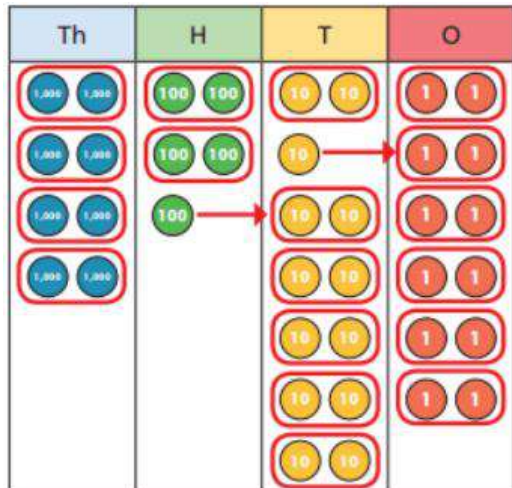
Language is important here. Children should consider 'How many groups of 4 tens can we make?' and 'How many groups of 4 ones can we make?'
Remainders can also be seen as they are left ungrouped.

$$856 \div 4$$





$$8532 \div 2$$



Understanding remainders

Understand remainders using concrete versions of a problem.

80 cakes divided into trays of 6.



80 cakes in total. They make 13 groups of 6, with 2 remaining.

Use short division and understand remainders as the last remaining 1s.

6 $\overline{) 80}$

Lay out the problem as short division.

T	O
10 10 10 10 10	

How many groups of 6 go into 8 tens?
There is 1 group of 6 tens.
There are 2 tens remaining.

6 $\overline{) 8} 20$

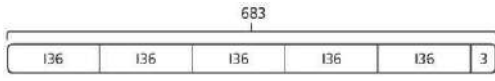
T	O
10 10 10	

How many groups of 6 go into 20 ones?
There are 3 groups of 6 ones.
There are 2 ones remaining.

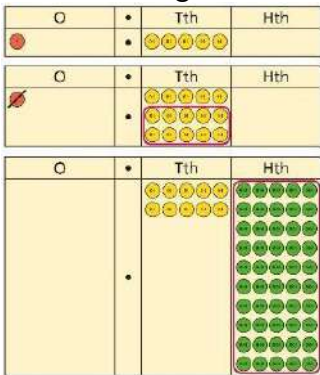
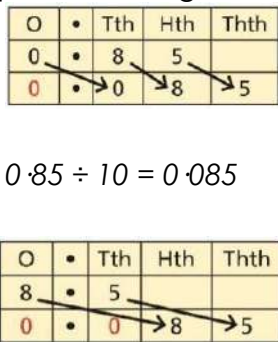
6 $\overline{) 8} 320$

T	O
10 10	10 10 10 10 10 10 10 10 10 10

In problem solving contexts, represent divisions including remainders with a bar model.



$683 = 136 \times 5 + 3$
 $683 \div 5 = 136 r 3$

<p>Dividing decimals by 10, 100 and 1,000</p>	<p>Understand division by 10 using exchange.</p> <p>2 ones are 20 tenths.</p> <p>20 tenths divided by 10 is 2 tenths.</p>	<p>Represent division using exchange on a place value grid.</p>  <p>1.5 is 1 one and 5 tenths. This is equivalent to 10 tenths and 50 hundredths. 10 tenths divided by 10 is 1 tenth. 50 hundredths divided by 10 is 5 hundredths. 1.5 divided by 10 is 1 tenth and 5 hundredths. $1.5 \div 10 = 0.15$</p>	<p>Understand the movement of digits on a place value grid.</p>  <p>$0.85 \div 10 = 0.085$</p> <p>$8.5 \div 100 = 0.085$</p>
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Year 6

Addition

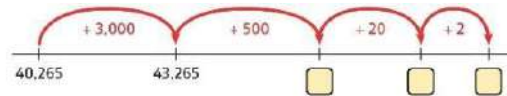
	<p>Concrete</p>	<p>Pictorial</p>	<p>Abstract</p>
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Comparing and selecting efficient methods

Represent 7-digit numbers on a place value grid, and use this to support thinking and mental methods.

M	HTh	TTh	Th	H	T	O
●●	●●●●	●	●	●●●		●

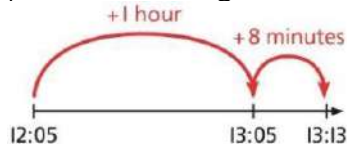
Discuss similarities and differences between methods, and choose efficient methods based on the specific calculation. Compare written and mental methods alongside place value representations.



TTh	Th	H	T	O
●●●●		●●	●●●●	●●●●
	●●●●	●●●●	●●	●●

TTh	Th	H	T	O
4	0	2	6	5
+	3	5	2	2

Use bar model and number line representations to model addition in problem-solving and measure contexts.



Use column addition where mental methods are not efficient. Recognise common errors with column addition.

$$32,145 + 4,302 = ?$$

TTh	Th	H	T	O
3	2	1	4	5
+	4	3	0	2
3	6	4	4	7


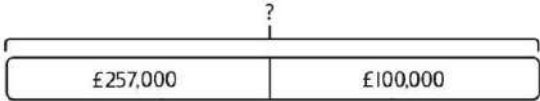
TTh	Th	H	T	O
3	2	1	4	5
+	4	3	0	2
7	5	1	6	5

Which method has been completed accurately?

What mistake has been made?

Column methods are also used for decimal additions where mental methods are not efficient.

H	T	O	Tth	Hth
1	4	0	0	9
+	4	9	8	9
1	8	9	9	8

<p>Selecting mental methods for larger numbers where appropriate</p>	<p>Represent 7-digit numbers on a place value grid, and use this to support thinking and mental methods.</p>  <p>$2,411,301 + 500,000 = ?$</p> <p><i>This would be 5 more counters in the HTh place.</i></p> <p><i>So, the total is 2,911,301.</i></p> <p>$2,411,301 + 500,000 = 2,911,301$</p>	<p>Use a bar model to support thinking in addition problems.</p>  <p>$257,000 + 99,000 = ?$</p> <p><i>I added 100 thousands then subtracted 1 thousand.</i></p> <p>$257 \text{ thousands} + 100 \text{ thousands} = 357 \text{ thousands}$</p> <p>$257,000 + 100,000 = 357,000$</p> <p>$357,000 - 1,000 = 356,000$</p> <p><i>So, $257,000 + 99,000 = 356,000$</i></p>	<p>Use place value and unitising to support mental calculations with larger numbers.</p> <p>$195,000 + 6,000 = ?$</p> <p>$195 + 5 + 1 = 201$</p> <p><i>195 thousands + 6 thousands = 201 thousands</i></p> <p><i>So, $195,000 + 6,000 = 201,000$</i></p>
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Subtraction

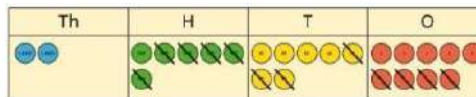
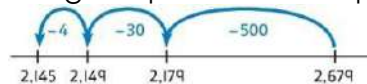
	Concrete	Pictorial	Abstract
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Comparing and selecting efficient methods

Use counters on a place value grid to represent subtractions of larger numbers.

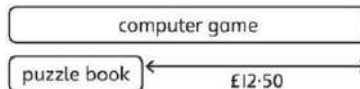


Compare subtraction methods alongside place value representations.



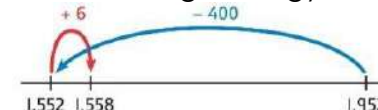
$$\begin{array}{r} \text{Th H T O} \\ 2\ 6\ 7\ 9 \\ -\ 5\ 3\ 4 \\ \hline 2\ 1\ 4\ 5 \end{array}$$

Use a bar model to represent calculations, including 'find the difference' with two bars as comparison.



Compare and select methods. Use column subtraction when mental methods are not efficient. Use two different methods for one calculation as a checking strategy.

$$\begin{array}{r} \text{Th H T O} \\ 1\ 5\ 5\ 8 \\ -\ 1\ 5\ 5\ 8 \\ \hline 3\ 9\ 4 \end{array}$$



Use column subtraction for decimal problems, including in the context of measure.

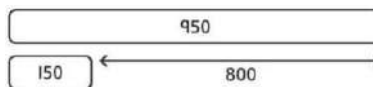
$$\begin{array}{r} \text{H T O} \cdot \text{Tth Hth} \\ 3\ 0\ 9 \cdot 6\ 0 \\ -\ 2\ 0\ 6 \cdot 4\ 0 \\ \hline 1\ 0\ 3 \cdot 2\ 0 \end{array}$$

Subtracting mentally with larger numbers

Use a bar model to show how unitising can support mental calculations.

$$950,000 - 150,000$$

That is 950 thousands - 150 thousands



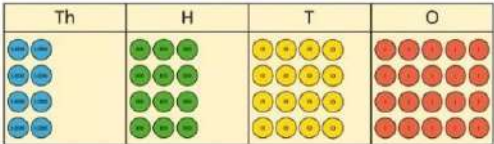
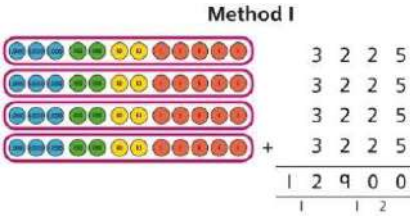
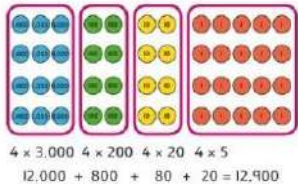
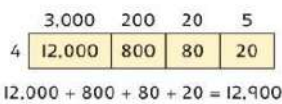
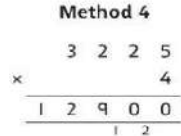
So, the difference is 800 thousands.

$$950,000 - 150,000 = 800,000$$

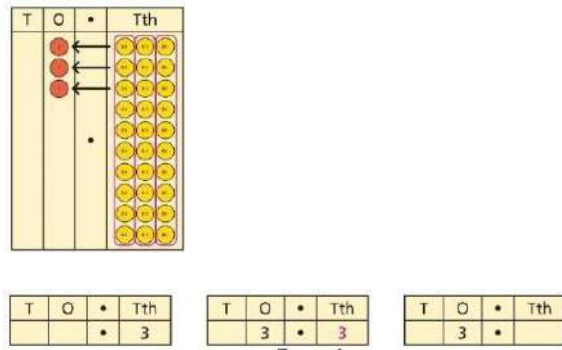
Subtract efficiently from powers of 10.

$$10,000 - 500 = ?$$

Multiplication

	Concrete	Pictorial	Abstract
<p>Multiplying up to a 4-digit number by a single digit number</p>	<p>Use equipment to explore multiplications.</p>  <p>4 groups of 2,345</p> <p>This is a multiplication:</p> $4 \times 2,345$ $2,345 \times 4$	<p>Use place value equipment to compare methods.</p> <p>Method 1</p>  <p>Method 2</p> 	<p>Understand area model and short multiplication.</p> <p>Compare and select appropriate methods for specific multiplications.</p> <p>Method 3</p>  <p>Method 4</p> 

<p>Multiplying up to a 4-digit number by a 2-digit number</p>		<p>Use an area model alongside written multiplication.</p> <p>Method 1</p> <table border="1" data-bbox="952 263 1344 391"> <tr> <td></td> <td>1,000</td> <td>200</td> <td>30</td> <td>5</td> </tr> <tr> <td>20</td> <td>20,000</td> <td>4,000</td> <td>600</td> <td>100</td> </tr> <tr> <td>1</td> <td>1,000</td> <td>200</td> <td>30</td> <td>5</td> </tr> </table> <table data-bbox="952 422 1220 718"> <tr> <td></td> <td>1</td> <td>2</td> <td>3</td> <td>5</td> <td></td> </tr> <tr> <td>x</td> <td></td> <td></td> <td>2</td> <td>1</td> <td></td> </tr> <tr> <td></td> <td></td> <td></td> <td></td> <td>5</td> <td>1 × 5</td> </tr> <tr> <td></td> <td></td> <td></td> <td>3</td> <td>0</td> <td>1 × 30</td> </tr> <tr> <td></td> <td></td> <td></td> <td>2</td> <td>0</td> <td>0</td> <td>1 × 200</td> </tr> <tr> <td></td> <td></td> <td>1</td> <td>0</td> <td>0</td> <td>0</td> <td>1 × 1,000</td> </tr> <tr> <td></td> <td></td> <td>1</td> <td>0</td> <td>0</td> <td></td> <td>20 × 5</td> </tr> <tr> <td></td> <td></td> <td>6</td> <td>0</td> <td>0</td> <td></td> <td>20 × 30</td> </tr> <tr> <td></td> <td></td> <td>4</td> <td>0</td> <td>0</td> <td></td> <td>20 × 200</td> </tr> <tr> <td></td> <td>2</td> <td>0</td> <td>0</td> <td>0</td> <td>0</td> <td>20 × 1,000</td> </tr> <tr> <td></td> <td>2</td> <td>5</td> <td>9</td> <td>3</td> <td>5</td> <td>21 × 1,235</td> </tr> </table>		1,000	200	30	5	20	20,000	4,000	600	100	1	1,000	200	30	5		1	2	3	5		x			2	1						5	1 × 5				3	0	1 × 30				2	0	0	1 × 200			1	0	0	0	1 × 1,000			1	0	0		20 × 5			6	0	0		20 × 30			4	0	0		20 × 200		2	0	0	0	0	20 × 1,000		2	5	9	3	5	21 × 1,235	<p>Use compact column multiplication with understanding of place value at all stages.</p> <table data-bbox="1556 263 1859 422"> <tr> <td></td> <td>1</td> <td>2</td> <td>3</td> <td>5</td> <td></td> </tr> <tr> <td>x</td> <td></td> <td></td> <td>2</td> <td>1</td> <td></td> </tr> <tr> <td></td> <td></td> <td></td> <td></td> <td>5</td> <td>1 × 1,235</td> </tr> <tr> <td></td> <td></td> <td></td> <td>2</td> <td>4</td> <td>7</td> <td>0</td> <td>0</td> <td>20 × 1,235</td> </tr> <tr> <td></td> <td></td> <td></td> <td>2</td> <td>5</td> <td>9</td> <td>3</td> <td>5</td> <td>21 × 1,235</td> </tr> </table> <table border="1" data-bbox="1556 486 1814 805"> <thead> <tr> <th></th> <th>TTh</th> <th>Th</th> <th>H</th> <th>T</th> <th>O</th> </tr> </thead> <tbody> <tr> <td></td> <td></td> <td>2</td> <td>7</td> <td>3</td> <td>9</td> </tr> <tr> <td>x</td> <td></td> <td></td> <td></td> <td>2</td> <td>8</td> </tr> <tr> <td></td> <td>2</td> <td>1</td> <td>9</td> <td>1</td> <td>2</td> </tr> <tr> <td>2</td> <td>5</td> <td>3</td> <td>7</td> <td></td> <td></td> </tr> <tr> <td>1</td> <td>5</td> <td>4</td> <td>7</td> <td>8</td> <td>0</td> </tr> <tr> <td></td> <td>7</td> <td>6</td> <td>6</td> <td>9</td> <td>2</td> </tr> </tbody> </table>		1	2	3	5		x			2	1						5	1 × 1,235				2	4	7	0	0	20 × 1,235				2	5	9	3	5	21 × 1,235		TTh	Th	H	T	O			2	7	3	9	x				2	8		2	1	9	1	2	2	5	3	7			1	5	4	7	8	0		7	6	6	9	2
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<p>Multiplying by 10, 100 and 1,000</p>	<p>Children use place value counters to represent multiplying a decimal number by 10, leading to an exchange being needed.</p> <p>Children see that when multiplying by 10, they exchange for a counter that goes in the place value column to the left. Children then explore how multiplying by 100 is the same as multiplying by 10 and then 10 again, so digits move two place value columns to the left. Finally, they look at multiplying by 1,000.</p>	<p>Understand how the exchange affects decimal numbers on a place value grid.</p>  <p>$0.3 \times 10 = 3$</p>	<p>Use knowledge of multiplying by 10, 100 and 1,000 to multiply by multiples of 10, 100 and 1,000.</p> <p>$8 \times 100 = 800$</p> <p>$8 \times 300 = 800 \times 3 = 2,400$</p> <p>$2.5 \times 10 = 25$</p> <p>$2.5 \times 20 = 2.5 \times 10 \times 2 = 50$</p>
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A Gattegno chart and plain counters in a place value chart are also used to help children with their understanding.

Use place value equipment to explore exchange in decimal multiplication.

Represent 0.3:

Multiply by 10.

Exchange each group of ten tenths.

$$0.3 \times 10 = ?$$

0.3 is 3 tenths.

10 × 3 tenths are 30 tenths.

30 tenths are equivalent to 3 ones.

1.21 × 10 = 12.1
 12.1 is 10 times the size of 1.21
 1.21 is one-tenth the size of 12.1

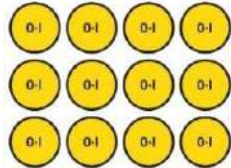
Gattegno Chart

0	80	90
7	8	9
.7	0.8	0.9
07	0.08	0.09

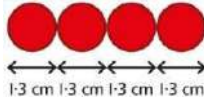
0.213 × 1,000 = 213
 213 is 1,000 times the size of 0.213. 213 is one-thousandth the size of 213

Multiplying decimals

Explore decimal multiplications using place value equipment and in the context of measures.



3 groups of 4 tenths is 12 tenths.
4 groups of 3 tenths is 12 tenths.



$$4 \times 1 \text{ cm} = 4 \text{ cm}$$

$$4 \times 0.3 \text{ cm} = 1.2 \text{ cm}$$

$$4 \times 1.3 = 4 + 1.2 = 5.2 \text{ cm}$$

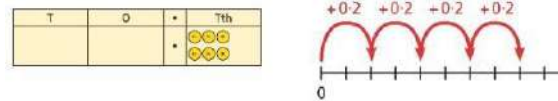
Represent calculations on a place value grid.

$$3 \times 3 = 9$$

$$3 \times 0.3 = 0.9$$

T	O	•	Tth
			● ● ●
			● ● ●
			● ● ●

Understand the link between multiplying decimals and repeated addition.



Use known facts to multiply decimals.

$$4 \times 3 = 12$$

$$4 \times 0.3 = 1.2$$

$$4 \times 0.03 = 0.12$$

$$20 \times 5 = 100$$

$$20 \times 0.5 = 10$$

$$20 \times 0.05 = 1$$

Find families of facts from a known multiplication.

I know that $18 \times 4 = 72$.

This can help me work out:

$$1.8 \times 4 = ?$$

$$18 \times 0.4 = ?$$

$$180 \times 0.4 = ?$$

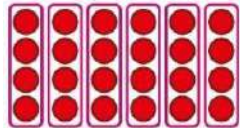
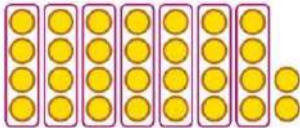
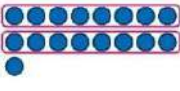
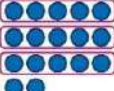
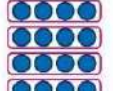
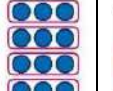
$$18 \times 0.04 = ?$$

Use a place value grid to understand the effects of multiplying decimals.

	H	T	O	•	Tth	Hth
2×3			6	•		
0.2×3			0	•	6	
0.02×3				•		

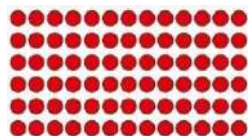
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Division

	Concrete	Pictorial	Abstract																																																		
Understanding factors	<p>Use equipment to explore different factors of a number.</p> <div style="display: flex; justify-content: space-around; align-items: center;"> <div style="text-align: center;">  <p>$24 \div 4 = 6$</p> </div> <div style="text-align: center;">  <p>$30 \div 4 = 7 \text{ remainder } 2$</p> </div> </div> <p><i>4 is a factor of 24 but is not a factor of 30.</i></p>	<p>Recognise prime numbers as numbers having exactly two factors. Understand the link with division and remainders.</p> <div style="display: flex; justify-content: space-around; align-items: center;"> <div style="text-align: center;">  <p>$17 \div 2 = 8 \text{ r } 1$</p> </div> <div style="text-align: center;">  <p>$17 \div 3 = 5 \text{ r } 2$</p> </div> <div style="text-align: center;">  <p>$17 \div 4 = 4 \text{ r } 1$</p> </div> <div style="text-align: center;">  <p>$17 \div 5 = 3 \text{ r } 2$</p> </div> </div>	<p>Recognise and know primes up to 100. Understand that 2 is the only even prime, and that 1 is not a prime number.</p> <table border="1" style="border-collapse: collapse; text-align: center; width: 100%;"> <tr><td>1</td><td>2</td><td>3</td><td>4</td><td>5</td><td>6</td><td>7</td><td>8</td><td>9</td><td>10</td></tr> <tr><td>11</td><td>12</td><td>13</td><td>14</td><td>15</td><td>16</td><td>17</td><td>18</td><td>19</td><td>20</td></tr> <tr><td>21</td><td>22</td><td>23</td><td>24</td><td>25</td><td>26</td><td>27</td><td>28</td><td>29</td><td>30</td></tr> <tr><td>31</td><td>32</td><td>33</td><td>34</td><td>35</td><td>36</td><td>37</td><td>38</td><td>39</td><td>40</td></tr> <tr><td>41</td><td>42</td><td>43</td><td>44</td><td>45</td><td>46</td><td>47</td><td>48</td><td>49</td><td>50</td></tr> </table>	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	37	38	39	40	41	42	43	44	45	46	47	48	49	50
1	2	3	4	5	6	7	8	9	10																																												
11	12	13	14	15	16	17	18	19	20																																												
21	22	23	24	25	26	27	28	29	30																																												
31	32	33	34	35	36	37	38	39	40																																												
41	42	43	44	45	46	47	48	49	50																																												

Dividing by a single digit

Use equipment to make groups from a total.



There are 78 in total.
There are 6 groups of 13.
There are 13 groups of 6.

(Also see link below – three digit divided by a single digit using long division – this will support when moving onto long division)

H	T	O	How many groups of 6 are in 100? $6 \overline{) 100}$
●	●● ●●	●●	
●	●● ●● ●● ●● ●● ●●	●●	
●	●● ●● ●● ●● ●● ●●	●●	How many groups of 6 are in 13 tens? $6 \overline{) 130}$
●	●● ●● ●● ●● ●● ●●	●●	
●	●● ●● ●● ●● ●● ●●	●● ●● ●● ●● ●● ●●	How many groups of 6 are in 12 ones? $6 \overline{) 122}$
●	●● ●● ●● ●● ●● ●●	●● ●● ●● ●● ●● ●●	

Th	H	T	O
●●●● ●●●●	●●● ●●●	●●● ●●● ●●● ●●● ●●● ●●●	●● ●●
●●●● ●●●●	●●● ●●●	●●● ●●● ●●● ●●● ●●● ●●●	●● ●●
●●●● ●●●●	●●● ●●●	●●● ●●● ●●● ●●● ●●● ●●●	●● ●●
●●●● ●●●●	●●● ●●●	●●● ●●● ●●● ●●● ●●● ●●●	●● ●●

$$8524 \div 4$$

Use short division to divide by a single digit.

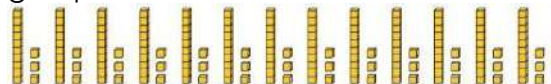
$$\begin{array}{r} 0 \\ 6 \overline{) 132} \end{array}$$

$$\begin{array}{r} 0 \ 2 \\ 6 \overline{) 132} \end{array}$$

$$\begin{array}{r} 0 \ 2 \ 2 \\ 6 \overline{) 132} \end{array}$$

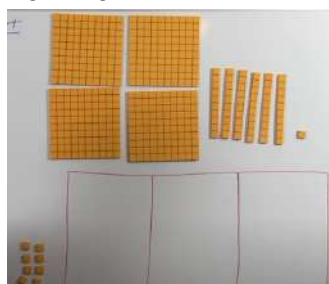
Dividing by a 2-digit number using long division

Use equipment to build numbers from groups.



182 divided into groups of 13.
There are 14 groups.

Sharing
 $461 \div 3$



1. Start by building 461 with dienes.



2. We have 4 hundreds. 3 can be shared equally but we can't share the last hundred so we

Progress to the expanded method that shows the multiples.

		0	3	6
1	2	4	3	2
	-	3	6	0
			7	2
	-		7	2
				0

- (x30) $12 \times 1 = 12$
- $12 \times 2 = 24$
- $12 \times 3 = 36$
- $12 \times 4 = 48$
- $12 \times 5 = 60$
- $12 \times 6 = 72$
- (x6) $12 \times 7 = 84$
- $12 \times 8 = 96$
- $12 \times 9 = 108$
- $12 \times 10 = 120$

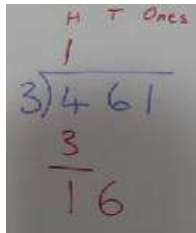
		0	4	8	9
15	7	3	3	5	
-	6	0	0	0	
	1	3	3	5	
-	1	2	0	0	
		1	3	5	
-		1	3	5	
				0	

- (x400) $1 \times 15 = 15$
- $2 \times 15 = 30$
- $3 \times 15 = 45$
- (x80) $4 \times 15 = 60$
- $5 \times 15 = 75$
- (x9) $10 \times 15 = 150$

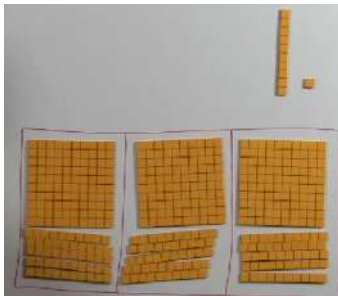
			2	4	r	1	2
1	5	3	7	2			
	-	3	0	0			
			7	2			
	-		6	0			
			1	2			

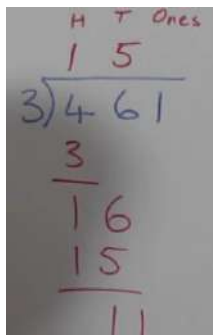
Children will interpret the remainder as the context requires- leave as a remainder, as a decimal or as a fraction.

need to exchange this for 10 tens. We now have 16 tens.

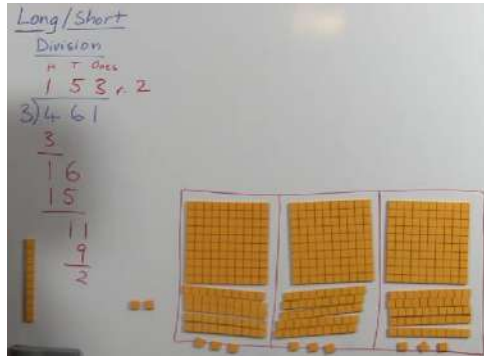

$$\begin{array}{r} \text{H} \quad \text{T} \quad \text{Ones} \\ 1 \\ \hline 3 \overline{) 461} \\ \underline{3} \\ 16 \\ \underline{15} \\ 1 \end{array}$$

3. Next, share the 16 tens equally between three. $5 \times 3 = 15$ with one ten left over.




$$\begin{array}{r} \text{H} \quad \text{T} \quad \text{Ones} \\ 1 \quad 5 \\ \hline 3 \overline{) 461} \\ \underline{3} \\ 16 \\ \underline{15} \\ 1 \end{array}$$

We then exchange the ten for ten ones so we end up with eleven ones. We share the eleven ones between three. $3 \times 3 = 9$ with two left over.



Concrete representation supports the reasoning behind the long division.

<https://www.youtube.com/watch?v=ElrA7BM4q6M>

Dividing by 10, 100 and 1,000

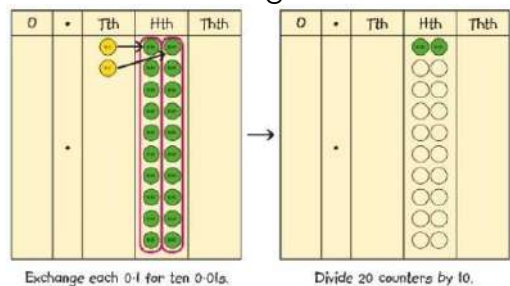
Children use place value counters to represent a decimal number being divided by 10. Using language such as "10 times the size" and "one-tenth of the size" will support children in their understanding.

Children recognise that dividing a number by 10 twice is the same as dividing the number by 100.

They then use a place value chart with counters (and then digits) to divide a number by 10, 100 or 1,000 by moving the counters the correct number of places to the right.

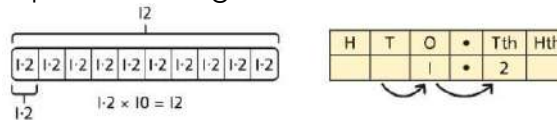
A Gattegno chart used will help children understand what happens to numbers as they are divided by powers of 10

Use place value equipment to explore division as exchange.

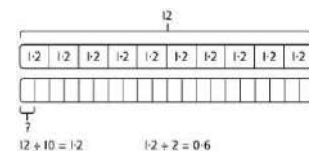


0.2 is 2 tenths.

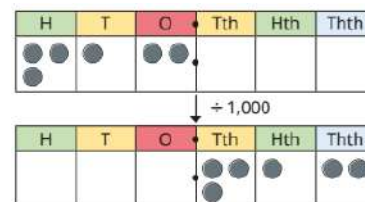
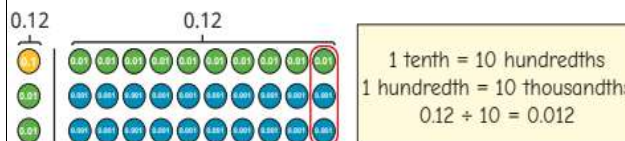
Represent division to show the relationship with multiplication. Understand the effect of dividing by 10, 100 and 1,000 on the digits on a place value grid.



Understand how to divide using division by 10, 100 and 1,000.



$12 \div 20 = ?$



$312 \div 1,000 = 0.312$
312 is 1,000 times the size of 0.312
0.312 is one-thousandth the size of 312

Use knowledge of factors to divide by multiples of 10, 100 and 1,000.

$40 \div 50 = \square$

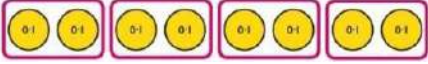
$40 \rightarrow \div 10 \rightarrow \div 5 \rightarrow ?$

$40 \rightarrow \div 5 \rightarrow \div 10 \rightarrow ?$

$40 \div 5 = 8$

$8 \div 10 = 0.8$

So, $40 \div 50 = 0.8$

	<p>2 tenths is equivalent to 20 hundredths. 20 hundredths divided by 10 is 2 hundredths.</p>										
<p>Dividing decimals</p>	<p>Use place value equipment to explore division of decimals.</p>  <p>8 tenths divided into 4 groups. 2 tenths in each group.</p>	<p>Use a bar model to represent divisions.</p> <table border="1" style="margin-left: auto; margin-right: auto;"> <tr> <td colspan="4" style="text-align: center;">0.8</td> </tr> <tr> <td style="text-align: center;">?</td> <td style="text-align: center;">?</td> <td style="text-align: center;">?</td> <td style="text-align: center;">?</td> </tr> </table> <p> $4 \times 2 = 8$ $8 \div 4 = 2$ So, $4 \times 0.2 = 0.8$ $0.8 \div 4 = 0.2$ </p>	0.8				?	?	?	?	<p>Use short division to divide decimals with up to 2 decimal places.</p> $\begin{array}{r} . \\ 8 \overline{) 4.24} \\ \underline{4 2} \\ 0 4 2 \\ \underline{0 4} 2 \\ 0 5 2 \\ \underline{0 5} 2 \\ 0 5 3 \\ \underline{0 5} 3 \end{array}$
0.8											
?	?	?	?								